Using a Hybrid Automated Valuation Model to Estimate Capital and Site Values

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Abstract: In recent years the use of Hybrid Automated Valuation Models has been widely discussed in the property taxation literature. Such models are now recognised in the IAAO's standard for AVM's. These models may produce superior results to simpler AVM's and may be particularly useful in a situation where improved properties need to be used to estimate site value. Given recent court decisions in Australia that seem to require valuers to consider sales with improvements when assessing site value in "thin markets", such models may prove to be a useful tool in mass appraisal. This paper examines the use of a hybrid model to estimate capital and site values for residential properties in a small pilot study in Adelaide, South Australia. The model uses both vacant land and improved residential sales in a single model to estimate site and capital values simultaneously. This initial research shows that such models may prove to be a useful addition to the methodologies used by property tax authorities in Australia.

Introduction

In recent years the use of hybrid Automated Valuation Models (AVM's) has been widely discussed in the property taxation literature as well as in many individual reports where the results of such models are used in jurisdictions for mass appraisals. Such models are now recognised in the International Association of Assessing Officers (IAAO) standard for AVM's. These models may produce superior results to simpler AVM's and may be particularly useful in a situation where improved properties need to be used to estimate site value. Given recent court decisions in Australia that seem to require valuers to consider sales with improvements when assessing site value in "thin markets", such models may prove to be a useful tool in mass appraisal. This paper examines the use of a hybrid model to estimate capital and site values for residential properties in a small pilot study in Adelaide, South Australia. The model uses both vacant land and improved residential sales in a single model to estimate both site and capital values.

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Hybrid Automated Valuation Models

The IAAO standards define an automated valuation model (AVM) as

"a mathematically based computer software program that produces an estimate of market value based on market analysis of location, market conditions, and real estate characteristics from information that was previously and separately collected. The distinguishing feature of an AVM is that it is a market appraisal produced through mathematical modelling. Credibility of an AVM is dependent on the data used and the skills of the modeller producing the AVM" (IAAO, 2003 pp148)

They further recognize that these may be in an additive, multiplicative or hybrid form where the hybrid form is a

"model that incorporates both additive and multiplicative components" (IAAO, 2003 pp150)

and that these are normally hedonic models which attempt

"to take observations on the overall good or service and obtain implicit prices for the goods and services. Prices are measured in terms of quantity and quality. When valuing real property, the spatial attributes and property specific attributes are valued in a single model. Calibration of the attribute components is performed statistically by regressing the overall price onto the characteristics." (IAAO, 2003 pp149)

In a study researching the valuation of land and improvements in the City of Philadelphia, McCain, Jensen et al. (2003) use some 40,000 arm's length transactions to develop a two stage hybrid model. The first stage involved estimating a neighbourhood index for each property which was then used as input to a hybrid regression model. The neighbourhood index was estimated from the residuals of a simple hedonic model (using building and site characteristics) and then using a Kriging process to smooth out the variation. This neighbourhood variable was then used with land area, liveable area and building condition in a non-linear regression. The hybrid model was specified as (op cit)

 $p = (b0(LiveableArea)^{b1}(Condition)^{b2}(Neighborhood)^{b3}) + (b4(LandArea)^{b5}(Neighborhood)^{b6})$

Where *p* is the price of the property.

This model is applied using both improved and unimproved sales and allows for the neighbourhood influence to be attached to both the land and improvements components at a different rate. Values for improved properties use the whole equation while vacant land estimates effectively use only the second component (since liveable area and condition are zero). This model proved to be effective even with a small set of descriptive variables. McCluskey, Deddis et al. (1998) discuss various methods of building spatial variation into mass appraisal. They discuss the problems of using submarket analysis where the submarkets often become small and the statistical analysis becomes unsound and biased (they do not discuss this in terms of non-statistical methods but the same problem applies). They then discuss the problems of using dummy variables for discrete locations such as suburbs. They point out that this "presupposes that the affect of location is uniform across all properties within a particular neighbourhood". This method also causes problems for mass appraisal authorities because of the lumpiness of assessments and broader conflicts. They suggest at more continuous approach using methods such as surface response analysis and the kriging method. These methods are applied through several of the standard GIS packages.

A study of three alternative models (additive, multiplicative and non-linear) was reported by O'Connor (2002) based on work in Calgary. They used a large geographical area and used some 35,000 records randomly split into about 4/5th for model building and 1/5th for testing. They used a two level cleaning process each involving the removal of the lowest and highest 2.5% of estimate to sale ratios. They use two methods to allow for location influences; a location value response surface (LVRS) based on median prices and one based on fixed neighbourhood boundaries. Models are generated for each of the three model types and using both locational methods. The results are compared using assessment ratio statistics the

coefficient of dispersion (COD), coefficient of variation (COV) and price-related differential (PRD) as specified by the IAAO Standards on Ratio Studies (1999). They found a multiplicative model with LVRS to be superior when using both the within model and hold out data with a COV of 7 and 7.91 respectively.

In a similar study involving Calgary, Gloudemans (2002, see also Gloudemans, 2002a) followed similar procedures but used more discriminating sales selection based on transaction characteristics as well as high AS ratios. They split the data into testing and model build subgroups of 5000 and 25,303 sales respectively using random selection. They then created additive (linear), multiplicative (log-linear) and Hybrid (non-linear) models. Location included in the model via a large number (hundreds) of neighbourhood dummies. The non-linear model is specified in a similar manner to that of McCain, Jensen et al. (2003) with the site and building parts being multiplicative and added together. They concluded that all three models produced good results but the multiplicative model produced the best results although they felt that it might not have produced the best results across the whole city and that the non-linear specification most closely fitted the appraisal theory.

Estimating Site and Capital Values

One important advantage of these hybrid models is that they may offer a suitable solution to the valuation of land for site value purposes in situations where the number of sales is low generally called a "thin market". In the Maurici Case (High Court of Australia, February 13, 2003) summarised by Collins (2003) and applauded by Robbins (2003), the valuer was criticised for failing to consider improved properties when estimating the unimproved value and relying upon a small number of sales from a very thin market. The relative judgments in this case will not be debated in this paper but the case has re-opened the debate about using such traditional methods as the cost approach. While it is clear some of the writers on this issue have a fundamental misunderstanding of market valuation and a naive understanding of the use of cost to estimate value, the opportunity to reopen the analysis of improved sales to value vacant sites in a quantitative manner should be welcomed by academics and practitioners. One particular use of such analysis is in the derivation of site values for rating and taxation purposes.

In Australia the basis for valuation for rating and taxation purposes varies from state to state. New South Wales and Queensland use unimproved value: Victorian councils have a choice of assessing capital value, net annual value or site value; Tasmania assesses capital improved value, land value and assessed annual value; Western Australia assess gross rental value, site value (urban), unimproved value (rural) and capital value (government owned properties) and South Australia asses both capital value and site value for every property. Generally site or unimproved value is used for land tax while the other bases may be used for other purposes. Site or unimproved value is assessed in all jurisdictions but is fraught with difficulties in many of the established urban (and rural) areas due to the low number of market transactions. While unimproved value is a hypothetical and non-market testable construct in most cases, its foundation is in the market for vacant rather than improved sales. If the findings of Maurici are accepted as reasonable then the scarce sales of vacant land may not be sufficient to indicate the true market value of vacant land (and therefore unimproved land) and transactions of improved properties should also be considered. Since the cost of construction rarely equals the added value of improvements (the added value tends to be either above or below the cost of construction depending on the relative supply-demand situation) this is not a suitable method for "splitting" improved sales prices into a land and building component. But this may be possible using market analysis that jointly considers the sales of both improved and vacant properties. A properly calibrated hybrid model may meet these demands. In South Australia where every property must be assessed for both capital and site value, such a hybrid model may serve the purpose of completing all valuations from a single model and lead to acceptable estimates of both site and capital value. It is with these aims in view that this research has been carried out.

Methodology

Study Area

This study is conducted in a small section of Metropolitan Adelaide incorporating nine suburbs. The area is located in the southern suburbs (see Appendix Figure 1) wedged between the sea to the west, hills to the east, a river and commercial district to the south and an industrial area to the north. The location contains a mixture of housing established over a 40 year period in a number of expanding developments. As a result some parts of the study area have predominantly improved sales and few vacant land sales while the newer locations have larger volumes of vacant land sales.

Study Period

The study is completed using data from 1998 ands 1999. This period was chosen for three reasons. It reflects a period of time when the residential property market in the area was relatively stable and therefore no requirements for time adjustments are necessary within the models. It is also a period when the quality of data is considered to be superior. In recent years there has been a concern that some property characteristic data held by the government (and made available to industry and research groups) has become less reliable as funding for appropriate staff is reduced. This data period is more likely to have a better quality of data. Thirdly this period was used in a pervious study of Adelaide that included results for parts of this location (Rossini, 1998) and provides valuable additional information. As in previous studies the data was broken into two groups. The first group would be used to create models and the second group to test the models. This is a standard holdout sample procedure typical of most forecasting and prediction methodologies and is designed to prevent overestimating the accuracy of the models where over-fitting occurs. For this study, designation of these two data sets was based on a logical rather then random approach. If the model were to be used to assess capital and site values then the normal procedure would be to use sales from one period to estimate the values for the forthcoming assessment period. In this study we assume that the task is to create capital and site assessments in 1999 using the data from the previous year (1998) and that the assessments are then evaluated at the end of 1999 using the sales that occur during the 1999 period as the accuracy test. While this is likely to cause some "on-average" under-assessments if prices have been increasing, it does create a more realistic model and test situation.

Data

For this study only detached houses and vacant land are used and allotment sizes are limited to those between 200 and 2000 sq metres. This would include the vast majority of all land uses in the study area. A large amount of data is available for each property but many of these are descriptors (such as the title reference) are not used in AVM's and some other variables are not collected for every property. One significant set of data not available on the sales history file is a geographic midpoint for each property (which might typically be generated from a GIS). These were added to the data set from a matched file of latitudes and longitudes. The variables listed in Table 1 are suitable for the use in the AVMs and were available for every property with the building characteristics being zero in the case of vacant properties.

Variable	Variable Name/Description
Sale Price	SalePrice
Sale Price	SaleDate
Longitude	Easting and converted to a simple grid reference (X)
Latitude	Northing and converted to a simple grid reference (Y)
Land Area	Larea
Building Area	Barea
Number of Main Rooms	Rooms
Building Condition Code	Condition
Building Age	Bage
Outer Wall cladding	Converted to Dummy Variables
Roof cladding	Converted to Dummy Variables
Building Style	Converted to Dummy Variables

Table 1 - Variables used in the AVM's

All relevant transactions were extracted from the sale history file and cleaned for observations with missing data or where the price was demonstrably incorrect. This was based on properties with a current A/S Ratio between .25 and 4 (the price is no more than 4 times or less than ¼ of the current assessed value). Unlike previous studies, properties that did not accurately model were not excluded. All data removed was on an a-priori basis rather the expost approach taken by both O'Conner and Gloudemans where properties that are poorly estimated in the models are removed. That approach will tend to overestimate the accuracy of the models as some of these will be properties that are genuine transactions with correct data but that the model is incapable of properly estimating. The likely cause being omitted variables. By removing such data the opportunities to investigate these omitted variables is lost and the accuracy of the model appears better both in terms of the model statistics and the test statistics where difficult to assess properties have been removed. The approach taken in this study is to remove only those observations that are clearly incorrect or where there is missing data making it impossible to use the observations. This means that the estimates of model accuracy become quite conservative and would only be improved by diligent sales analysis and data rechecking. These would normally be carried out by a rating authority in the process of mass appraisal. As a result it is likely that a number of gross outliers will appear in the tests assessments that would not occur in a true mass appraisal.

After this basic cleaning process there were 2300 observations with 47% for the model building and 53% for model testing. A break down of these observations by suburbs and land use is shown in Table 3 and by model-test and land use in Table 4.

Modelling

The following is a summary of the process was used in the muti-stage modelling.

- Step 1. Split the data into model and test data
- Step 2. Use the model data to develop linear and log-linear AVM's using the building and site characteristics. Select the best model and save the standardised residuals.
- Step 3. Using the standardised residuals from step 2 use the latitude and longitude as and X and Y coordinate and polynomial expansions of these variables to establish a location value response surface.
- Step 4. Using the surface in step 3 estimate a new locational variable (LOCATION) for all observations. This location variable should account for major locational effects but ignore more local neighbourhood effects.

- Step 5. Use the model data to develop linear, log-linear and non-linear (hybrid) models using the location, site and building characteristics. Select the best model and save the residuals.
- Step 6. Using the residuals from step 2 use a coordinate (X-Y) grid to find smoothed residual effects using a kriging approach.
- Step 7. Using the "kriged" coordinate grid in step 3 estimate a new neighbourhood variable (N-B-HOOD) for all observations. This variable should account for localised neighbourhood effects that exist in addition to the more general locational effects.
- Step 8. Use the model data to develop linear, log-linear and non-linear (hybrid) models using the location, neighbourhood, site and building characteristics.
- Step 9. Estimate the value for all properties using each of the three models developed at steps 5 and 8.
- Step 10. Calculate accuracy statistics for model and test data and for both vacant and improved properties for each of the models in step 9. The test statistics used for this study are the mean absolute percentage error which is a standard forecast accuracy test, the mean, coefficient to variation of the assessment of sale price (A/S) ratio. These are two of the standard tests defined in the IAAO standard for ratio studies (IAAO 1999).

Results

Model estimates

The results of the various regression models are shown in the appendix. Models were estimated using a stepwise approach with manual manipulations to prevent multicollinearity becoming an issue. Table 5 shows the linear regression using the site and building characteristics while Table 6 shows the equivalent log-linear model. Each model uses similar variables in particular the building and land areas and building age and a number of dummy variables. In each case the variance inflation factor (VIF) indicates that there is no significant multicollinearity between any of the variables. Both models produce an R squared value of around .85 and highly significant F values. The log-linear model produces slightly superior forecasts with a higher F value and was selected as the superior model. The residuals from this model were then used in the second stage regression to estimate the locational factors using the location value response surface. The surface was estimated with an OLS estimate using a quartic order polynomial expansion of the X and Y coordinates that were derived from each properties latitude and longitude and the standardised residuals from the previous model. The results are shown as Table 7 and a graphical representation of the value surface is shown in Figure 2. The surface shows the expected responses with higher values along the coast line to the west and along the elevated hills area to the east. Values in the central area and near the industrial estate are lower with the lowest value being associated with a newer estate located near the commercial-shopping area to the south. The model shows an expected low R squared value of .217 but which is still statistically significant at greater than a 99% level of confidence. This model was used to estimate the new location variable for each property based on the properties relative position on the location value response surface. This variable was added to the data set and the models re-estimated with the inclusion of the location variable. Table 8 shows the results for the linear model and Table 9 the model for the log-linear model. In each case the model improved in its explanatory power with an increased R squared and F ratio and decreased standard error of the estimate. The log-linear model now shows clear superiority however this is to be expected since the added locational variable was estimated from the log-linear residuals at the previous step.

A non-linear model was also estimated. Since the non-linear model uses a generalised least squares approach (as opposed to ordinary least squares) and this is based on an iterative

approach, it is necessary to provide starting estimates for all the model parameters (regression coefficients). These starting values were estimated from 2 preliminary regression modles firstly using vacant land sales and then using the improved sales. In each case a log-log form was used to arrive at these starting values. This followed the procedure taken by McCain, Jensen et al. (2003). The estimates for the non-linear (hybrid) model are shown in Table 10 The model is quite robust but has no better explanatory power than the linear and log-linear models. The residuals from the log-linear model were then used to estimate the neighbourhood variations using a kriging approach.

The three models were then re-estimated using variables form the previous stage and the new neighbourhood variable. Results for these models are shown as linear (Table 11) log-linear (Table 12) and non-linear (Table 13). Again each model showed a statistical improvement from the previous steps with increases in R squared and F ratios and decreases in the standard errors of the estimate. Again each model showed about the same explanatory power.

Assessment estimates and accuracy

While the statistical testing of models is useful, the only true test of a predictive model is to conduct out of sample testing. Table 2 shows the results for the predictive accuracy of assessments using the linear, log-linear and non-linear models with the inclusions of the locational and neighbourhood variables estimated at steps 5 and 8 and described earlier as step 9 in the methodology. The accuracy is shown separately for the improved dwellings and for the vacant properties and for the properties used within the models (1998 sales) and those held out of the model (1999 sales).

		Abs	olute			
Data	Model	Percenta	ige Errors	A/S Ra	atio Stati	stics
Data	Woder	Mean	within			
		(MAPE)	10%	Average	St Dev	COV
	Linear	9.9%	61.1%	1.016	0.128	12.631
Dwallingo	Linear with N-Hood	9.7%	66.1%	1.008	0.124	12.291
Model Data	Log-Linear	9.6%	61.1%	1.041	0.126	12.072
(1998)	Log-Linear with N-Hood	6.8%	83.7%	1.071	0.129	12.042
(1000)	Hybrid	9.7%	64.8%	1.031	0.111	10.734
	Hybrid with N-Hood	7.4%	79.4%	1.033	0.110	10.622
	Linear	10.6%	54.2%	0.967	0.127	13.151
Dwallingo	Linear with N-Hood	11.6%	50.6%	0.957	0.125	13.054
Tost Data	Log-Linear	10.6%	54.6%	0.985	0.126	12.781
(1999)	Log-Linear with N-Hood	10.0%	56.6%	1.027	0.145	14.143
(1000)	Hybrid	9.6%	61.4%	0.986	0.125	12.694
	Hybrid with N-Hood	9.7%	60.7%	0.988	0.127	12.879
	Linear	10.3%	57.5%	1.001	0.129	12.837
Vecent	Linear with N-Hood	10.1%	66.7%	1.012	0.169	16.738
Vacant Model Data	Log-Linear	13.4%	43.1%	1.065	0.128	11.990
(1998)	Log-Linear with N-Hood	12.3%	51.7%	1.028	0.151	14.652
(1000)	Hybrid	10.1%	60.9%	1.028	0.165	16.026
	Hybrid with N-Hood	10.8%	59.8%	1.072	0.134	12.478
	Linear	14.0%	42.0%	0.900	0.262	29.368
	Linear with N-Hood	13.7%	46.6%	0.941	0.284	30.213
Vacant	Log-Linear	16.2%	35.8%	0.963	0.291	30.187
Test Data	Log-Linear with N-Hood	16.0%	38.1%	0.942	0.282	29.918
(1999)	Hybrid	13.2%	48.9%	0.964	0.290	30.058
	Hybrid with N-Hood	13.5%	49.4%	0.968	0.294	30.331

Table 2 - Accuracy	v toete for all	models for in	and out of se	ample data
Table 2 - Accurac	y lesis ioi all		and out of Se	ample uala.

Improved properties

The results for the improved dwellings shows that the models including the neighbourhood variable were significantly better for the log-linear and hybrid models when considering the in sample data but when using the holdout or test data, these models did not perform better. This suggests that that the use of the neighbourhood variable based on the kriging of the residuals does not improve the predictive accuracy of the models and that the original model is over-fitted. The out of sample tests for dwellings show that the hybrid model does produce superior assessment although the addition of the neighbourhood variables does not improve the model. The accuracy of these assessments is comparable to current assessed values in South Australia. In his paper discussing the accuracy requirements of automated and intelligent systems, Rossini (1999) analyses the accuracy of assessed values for detached dwellings over the whole Adelaide metropolitan area for sales within a 3 month period in 1998. He found the mean error of -8.48% suggesting a systematic underestimation of values with a MAPE of 11.47% and only 50.8% of values being within a 10% margin of errors. After correcting for the systematic underestimation (which has not been carried out in this study) the results showed an MAPE of 9.53% with 62.5% of values being with the 10% margin for error. This is consistent with the results from the hybrid model. This is impressive when considering that these estimates are based on a single model and where sales circumstances and the physical data have not been validated. Typical sales analysis and data validation would significantly improve these results.

Vacant Properties

The results for the vacant land models are less accurate. The estimates for the properties within the model are less accurate than those for the improved properties with the basic linear and hybrid models (without the neighbour hood) producing the best and similar results. The accuracy of the predictions for the out of sample hold out properties are considerably worse than for the improved properties. Some of this is due to the higher levels of growth in vacant land prices. While the A/S ratios are just below 1 for the improved test data suggesting that prices may have risen by around 2 %, the A/S ratios for the vacant land test data are considerably less than 1 for all models and would suggest that prices had risen by about 4 to 6 percent. This would explain the higher MAPE and lower numbers of estimates within 10% however it does not explain why the standard deviation and hence the COV are so much greater. These results are probably what we would expect given that we have only one property descriptor (land area) as well as the wider location variables. There are also less observations and many of the estimates will be based on locations where there are very few sales. While these errors cast some doubt on the suitability of using such a mode for site value estimates (the calculation can be applied to the improved properties to estimate site value as well) these values are at least highly consistent and could be defended as using all available sales in the location. Broader locational influences are estimated better through the use of the improved sales as well. The resultant site values would show sensible patterns for land size and location but would lack the definition that other qualitative factors might provide.

Improvements to the models

As mentioned earlier the validation of the circumstances of sale and of the physical characteristics of the properties involved would lead to significant increases in predictive accuracy. In each category a small number of observations with very large errors contributes to both poor models and lower than expected overall assessment accuracy. Adoption of the ex post procedures used by both O'Conner and Gloudemans would undoubtable improve the tests statistics but may not be reflected in actual final assessments.

One clear problem of the models is the omission of some key variables. In particular the addition of a site features variable would contribute to the model. The data set contained only one useful indicator of site value which was the land area. While this is undoubtedly important this suggests that all vacant properties of the same size and in the same general location will sell for the same amount. Anecdotally we know that issues such as access, corner allotments and main roads will also significantly affect values. For improved properties other site features

such as gardens, shedding and features such as swimming pools will also affect value. The inclusion of other variables is supported by Rossini (1998) who found that in Morphett Vale and Woodcroft, regression models were improved by adding additional data such as a site features rating to that held on the standard sales history file.

Some location and neighbourhood factors could also be considered differently. While the kriging approach should allow for local variations the averaging used in this method would probably dampen highly specific relationships such as main roads and coastal frontage. Future research will investigate other ways to incorporate some of these issues.

Conclusions

This study aimed to investigate the usefulness of hybrid AVM's to estimate both capital and site values. The results suggest that these models would be a useful addition to the armoury of techniques available for mass appraisal. While the predictive accuracy of the hybrid model is only slightly better than the more simple models, they have the added advantage of being specified in a manner that is more theoretically acceptable to some analysts. The model can be used to estimate both capital and site values with good accuracy and may be particularly useful for estimating site values in situations where there is a scarcity of vacant land transactions.

While the results of this study suggest less accurate results than some previous studies using the same methods, this is probably due to the different data cleaning that is used. In this study very limited data cleaning was used resulting in a conservative estimate of the accuracy that could be achieved with these models given the types of in field sales analysis typically conducted prior to a mass appraisal.

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Appendix



Figure 1 - Metropolitan Adelaide showing Study Area

Suburb		Land Use		Total
	Dwelling - Established	Dwelling - not Established	Vacant	
CHRISTIE DOWNS	140	1	0	141
CHRISTIES BEACH	156	1	9	166
НАСКНАМ	122	2	5	129
HACKHAM WEST	102	0	0	102
HUNTFIELD HEIGHTS	122	6	4	132
MORPHETT VALE	783	14	56	853
ONKAPARINGA HILLS	61	13	25	99
O'SULLIVAN BEACH	58	0	1	59
WOODCROFT	290	79	250	619
Total	1834	116	350	2300

Table 3 Summary of data by Suburb and Land Use

Table 4 Summary of data by type and year

Туре	Year of Sale	Frequency	Percent
Dwelling - Model	1998	898	39.0%
Dwelling - Test	1999	1052	45.7%
Vacant - Model	1998	174	7.6%
Vacant - Test	1999	176	7.7%
Total		2300	100.0%

Table 5 Model Summary (Linear Regression using Site and Building Characteristics)

Model	R	R Square	Adjusted R Square	Std. Error of the Estimate				
12	0.922	0.851	0.850	12338.672				
ANOVA								
M - 1 - 1		Sum of	.16	M	-	0.1		
woder		Squares	ar	Mean Square	F	Sig.		
12	Regression	1.98762E+12	12	1.65635E+11	503.785	0.000		
	Residual	3.48179E+11	1059	328781273.6				
	Total	2.3358E+12	1071					
Coefficier	nts(a)							
Model		Unstandardized	ł	Standardized	+	Sia	Collingarity	Statistics
MOUEI		Coemcients		Dete	ı	Sig.	Talaranaa	
		В	Sta. Error	Beta			loierance	VIF
12	(Constant)	24662.818	1144.551		21.548	0.0000		
	BArea	494.250	5.037	0.876	98.132	0.0000	0.818	1.222
	Bage	-630.386	23.990	-0.242	-26.277	0.0000	0.767	1.303
	SAHT	-9517.880	738.456	-0.111	-12.889	0.0000	0.886	1.129
	LArea	22.887	1.690	0.117	13.540	0.0000	0.872	1.147
	Villa	11209.567	1891.867	0.052	5.925	0.0000	0.837	1.195
	Shack	23426.363	4052.125	0.048	5.781	0.0000	0.931	1.074
	GIRoof	4967.183	1113.106	0.040	4.462	0.0000	0.830	1.205
	Colonial	4957.720	1325.152	0.031	3.741	0.0002	0.962	1.040
	Tudor	17323.570	6199.690	0.023	2.794	0.0052	0.992	1.008
	Ranch	-4944.454	1868.296	-0.021	-2.647	0.0082	0.989	1.012
	Bungalo	9447.283	3922.537	0.020	2.408	0.0161	0.994	1.006
	Spanish	-6298.892	2856.816	-0.018	-2.205	0.0276	0.990	1.010

a Dependent Variable: SalePrice

Table 6 Model Summary (Log-Linear Regression using Site and Building Characteristics)

Model	R	R Square	Adjusted R Square	Std. Error of the Estimate				
10	0.922	0.850	0.849	0.158				
ANOVA								
Model		Sum of Squares	df	Mean Square	F	Sig.		
10	Regression	321.936236	10	32.1936236	601.384	0.000		
	Residual	56.79802052	1061	0.053532536				
	Total	378.7342565	1071					
Coefficie	nts(a)							
Model		Unstandardize Coefficients	d	Standardized Coefficients	t	Sig.	Collinearity	Statistics
		В	Std. Error	Beta			Tolerance	VIF
10	(Constant)	10.427	0.015		678.571	0.0000		
	BArea	0.005	0.000	0.652	27.639	0.0000	0.118	1.482
	SAHT	-0.101	0.009	-0.093	-10.768	0.0000	0.887	1.128
	Averoomsize	0.012	0.001	0.267	11.085	0.0000	0.113	1.849
	Bage	-0.004	0.000	-0.122	-12.341	0.0000	0.676	1.480
	LArea	0.000	0.000	0.094	10.639	0.0000	0.837	1.195
	Shack	0.214	0.052	0.035	4.137	0.0000	0.931	1.074
	Villa	0.066	0.024	0.024	2.702	0.0069	0.829	1.206
	Colonial	0.039	0.017	0.019	2.296	0.0218	0.963	1.038
	GIRoof	0.030	0.014	0.019	2.102	0.0357	0.830	1.204
	tfwall	-0.315	0.159	-0.016	-1.981	0.0477	0.979	1.022
•	Dependent \/e		~~					

a Dependent Variable: InSalePrice

Model	R	R Square	Adjusted R Square	Std. Error of the Estimate			
12	0.466	0.217	0.213	0.885			
ANOVA	(b)						
Model		Sum of Squares	df	Mean Square	F	Sig.	
12	Regression	496.10164	12	41.3418034	24.446		1.043E-48
	Residual	1790.8984	1059	1.691122152			
	Total	2287	1071				
Coeffici	ents(a)						
Model		Unstandardized	d Coefficients	Standardized Coefficients	t	Sig.	
		B S	td. Error	Beta			
12	(Constant)	-0.147	1.071		-0.137		0.8910
	XCord	-0.591	0.388	-1.492	-1.521		0.1285
	YCord	0.278	0.477	0.454	0.584		0.5591
	XSqd	0.084	0.041	2.360	2.063		0.0392
	XbyY	0.173	0.139	1.658	1.239		0.2153
	YSqdX	-0.041	0.015	-2.211	-2.729		0.0064
	YCubed	0.002	0.021	0.131	0.108		0.9136
	XSqdYSqd	-0.004	0.005	-1.300	-0.783		0.4339
	XCubYSqd	0.001	0.000	1.427	1.517		0.1295
	XSqdYCub	0.001	0.000	1.088	2.441		0.0147
	XCubY	-0.003	0.001	-1.407	-2.665		0.0078
	XQuart	0.000	0.000	-0.232	-0.681		0.4957
	YQuart	0.000	0.002	-0.134	-0.194		0.8463

Table 7 Model Summary (Linear Regression using Polynomial Expansions of Latitude and Longitude)

Dependent Variable: Standardized Residual а

Table 8 Model Summary (Linear Regression using Site and Building Characteristics and Location)

Model	R	R Square	Adjusted R Square	Std. Error of the Estimate				
11	0.936	0.877	0.875	10773.551				
ANOVA	.(I)							
		.						
Model		Sum of	df	Moon Square	F	Sia		
	Dograaaian		ui		F	Siy.		
11	Regression	0.73093E+11	11	79420000070	004.303	0		
	Residual	1.23034E+11	1060	116069400.8				
o "···	Iotal	9.96727E+11	1071					
Coeffici	ents(a)	Unotondordizo	4	Standardized			Collingarity	
Model		Coefficients	1	Coefficients	t	Sia.	Statistics	
		В	Std. Error	Beta	-	3-	Tolerance	VIF
11	(Constant)	3288.657	1950.173		1.686	0.0920		
	BArea	504.092	8.383	0.948	60.131	0.0000	0.468	2.136
	LOCATION	14950.181	764.380	0.234	19.559	0.0000	0.815	1.227
	SAHT	-11415.823	952.088	-0.137	-11.990	0.0000	0.887	1.128
	LArea	17.737	2.138	0.094	8.296	0.0000	0.914	1.094
	Contemp	-15802.858	2231.679	-0.080	-7.081	0.0000	0.919	1.089
	Villa	10144.727	2584.668	0.045	3.925	0.0001	0.885	1.130
	TiledRof	-6296.259	1250.701	-0.088	-5.034	0.0000	0.380	2.633
	Shack	-15141.505	6050.080	-0.030	-2.503	0.0125	0.796	1.257
	Auster	-16247.475	4149.224	-0.043	-3.916	0.0001	0.969	1.031
	Tudor	27199.557	7646.079	0.038	3.557	0.0004	0.995	1.005
	ImTilRof	-12519.293	5454.944	-0.028	-2.295	0.0219	0.784	1.276
а		ariable. SalePric	۵					

а Dependent Variable: SalePrice

Table 9 Model Summary (Log-Linear Regression using Site and Building Characteristics and Location)

Model	R	R Square	Adjusted R Square	Std. Error of the Estimate			Collinearity	
12	0.947	0.897	0.896	0.129	t	Sig.	Statistics	
ANOVA	.(m)					-		
		Sum of						
Model		Squares	df	Mean Square	F	Sig.		
12	Regression	153.093375	12	12.75778125	766.413	0		
	Residual	17.62821316	1059	0.016646094				
	Total	170.7215882	1071					
Coeffici	ents(a)							
		Unstandardize	d	Standardized			Collinearity	
Model		Coefficients	o	Coefficients	t	Sig.	Statistics	
		В	Std. Error	Beta			Tolerance	VIF
12	(Constant)	10.047	0.025		399.394	0.0000		
	BArea	0.004	0.000	0.601	20.336	0.0000	0.112	1.963
	LOCATION	0.204	0.009	0.244	21.596	0.0000	0.765	1.307
	Condition	0.034	0.003	0.251	9.688	0.0000	0.145	2.900
	SAHT	-0.158	0.012	-0.145	-13.511	0.0000	0.843	1.187
	LArea	0.000	0.000	0.108	10.231	0.0000	0.882	1.133
	Contemp	-0.147	0.026	-0.057	-5.651	0.0000	0.966	1.036
	Villa	0.117	0.030	0.040	3.881	0.0001	0.939	1.064
	Shack	-0.236	0.065	-0.036	-3.611	0.0003	0.980	1.021
	Averoomsize	0.005	0.002	0.129	3.503	0.0005	0.072	1.810
	Auster	-0.170	0.049	-0.034	-3.449	0.0006	0.981	1.019
	Tudor	0.203	0.092	0.022	2.216	0.0269	0.992	1.008
	tfwall	-0.291	0.132	-0.022	-2.197	0.0282	0.952	1.050

a Dependent Variable: InSalePrice

Table 10 Model Summary (Nonlinear Regression using Site and Building Characteristics and Location)

Nonlinear Regression Summary Statistics Dependent Variable SalePrice

R squared = 1 - Re	sidual	SS / Corrected SS =	.89354			
ANOVA						
Source			DF		Sum of Squares	Mean Square
Regression				15	7.84952E+12	5.23302E+11
Residual				1057	1.0449E+11	98855616.04
Uncorrected		Total		1072	7.95402E+12	
(Corrected Total)	1071	981468279684				
Nonlinear Regressio	n Equa	ation				

$$\label{eq:predSalePrice} \begin{split} & \text{PredSalePrice} = (b0^*\text{LOCATION} ** b1^*\text{LAREA} ** b2) + ((b4^*\text{BArea} ** b5^*\text{BAge} ** b6^*\text{Condition} ** b16)^*(b9^{**}\text{SAHT} *b10^{**}\text{AUSTER} *b11^{**}\text{Contemp} *b12^{**}\text{shack} *b13^{**}\text{bungalo} *b14^{**}\text{tudor} *b15^{**}\text{villa})) \;. \end{split}$$

	Asymptotic 95 %			
	Asymptotic	Confidence	Interval	
Parameter	Estimate	Std. Error	Lower	Upper
b0	1597.733	0.028	1597.677	1597.788
b1	0.383	0.010	0.364	0.403
b2	0.474	0.032	0.410	0.537
b4	145.154	0.056	145.045	145.264
b5	1.012	0.037	0.940	1.084
b6	-0.143	387.773	-761.034	760.749
b9	0.761	0.155	0.458	1.065
b10	0.985	0.000	0.985	0.985
b11	0.837	0.137	0.569	1.105
b12	0.770	45.318	-88.154	89.694
b13	0.954	0.113	0.731	1.176
b14	1.334	0.020	1.295	1.374
b15	1.134	0.029	1.077	1.191

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b16	0.669	0.043	0.584	0.754

Table 11 Model Summary	/ (Linear Regressior	n using Site and Building	Characteristics, Location	and Neighborhood)
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Model	R	R Square	Adjusted R Square	Std. Error of the Estimate				
13	0.960	0.921	0.920	8637.768				
ANOVA								
		Sum of						
Model		Squares	df	Mean Square	F	Sig.		
13	Regression	9.17788E+11	13	70599094734	946.228	0.000		
	Residual	78938484167	1058	74611043.64				
	Total	9.96727E+11	1071					
Coefficie	ents(a)							
				Standardized				
Model		Unstandardized	d Coefficients	Coefficients	t	Sig.	Collinearity	Statistics
		В	Std. Error	Beta			Tolerance	VIF
13	(Constant)	-17136.827	1683.334		-10.180	0.0000		
	BArea	486.617	6.039	0.916	80.585	0.0000	0.580	1.724
	LOCATION	16180.081	591.855	0.253	27.338	0.0000	0.874	1.145
	N_B_HOOD	203885.439	8315.621	0.214	24.518	0.0000	0.981	1.019
	SAHT	-13913.060	925.795	-0.167	-15.028	0.0000	0.603	1.659
	LArea	17.739	1.719	0.094	10.319	0.0000	0.909	1.100
	Contemp	-16630.568	1897.315	-0.084	-8.765	0.0000	0.817	1.224
	Auster	-22297.931	3488.700	-0.059	-6.391	0.0000	0.882	1.134
	Shack	-25702.320	4404.492	-0.051	-5.835	0.0000	0.965	1.036
	GIRoof	4497.431	1356.522	0.036	3.315	0.0009	0.646	1.549
	Tudor	25170.656	6151.148	0.036	4.092	0.0000	0.988	1.012
	Bungalo	-12703.031	3622.196	-0.031	-3.507	0.0005	0.953	1.049
	Villa	5357.961	2254.861	0.024	2.376	0.0177	0.748	1.337
	Convent	-1926.83172	813.254135	-0.031566246	2.3692861	0.0180012	0.4217122	2.3712854
а	Dependent Vari	able: SalePrice						

Table 12 Model Summary (Log-Linear Regression using Site and Building Characteristics, Location and Neighborhood)

Model	R	R Square	Adjusted R Square	Std. Error of the Estimate				
13	0.962	0.926	0.925	0.109				
ANOVA	.(n)							
		Sum of						
Model		Squares	df	Mean Square	F	Sig.		
13	Regression	158.1221213	13	12.1632401	1021.369	0.000		
	Residual	12.59946684	1058	0.011908759				
	Total	170.7215882	1071					
Coeffici	ents(a)							
		Unstandardized	b	Standardized		-		.
Model		Coefficients		Coefficients	t	Sig.	Collinearity	Statistics
		В	Std. Error	Beta			Tolerance	VIF
13	(Constant)	9.840	0.024		418.217	0.0000		
	BArea	0.004	0.000	0.595	23.789	0.0000	0.112	2.965
	LOCATION	0.213	0.008	0.255	26.645	0.0000	0.763	1.311
	N_B_HOOD	2.164	0.105	0.174	20.549	0.0000	0.976	1.024
	Condition	0.040	0.003	0.295	13.397	0.0000	0.144	2.965
	SAHT	-0.164	0.010	-0.151	-16.559	0.0000	0.842	1.188
	LArea	0.000	0.000	0.106	11.975	0.0000	0.882	1.133
	Contemp	-0.157	0.022	-0.060	-7.113	0.0000	0.965	1.036
	Shack	-0.297	0.055	-0.045	-5.371	0.0000	0.977	1.024
	Auster	-0.219	0.042	-0.044	-5.245	0.0000	0.978	1.022
	Averoomsize	0.004	0.001	0.106	3.400	0.0007	0.072	1.828
	Villa	0.077	0.025	0.026	3.013	0.0026	0.934	1.071
	tfwall	-0.311	0.112	-0.024	-2.780	0.0055	0.952	1.050
	Tudor	0.206	0.078	0.022	2.659	0.0080	0.992	1.008
•	Dependent Varial							

a Dependent Variable: InSalePrice

Table 13 Model Summary (Nonlinear Regression using Site and Building Characteristics, Location and Neighborhood)

Nonlinear Regression Summary Statistics Dependent Variable SalePrice

R squared = 1 - Residual SS / Corrected SS = .92569

ANOVA

Source			DF	Sum of Squares	Mean Square
Regression			17	7.88108E+12	4.63593E+11
Residual			1055	72930873130	69128789.7
Uncorrected		Total	1072	7.95402E+12	
(Corrected Total)	1071	981468279684			

Nonlinear Regression Equation

PredSalePrice = (b0*LOCATION ** b1*LAREA ** b2*N_B_HOOD ** b3) +((b4*BArea ** b5*BAge**b6*N_B_HOOD**b8*Condition**b16) *(b9**SAHT*b10**AUSTER*b11**Contemp*b12**shack*b13**bungalo*b14**tudor*b15**villa)).

	Asymptotic 95 %			
	Asymptotic	Confidence	Int	erval
Parameter	Estimate	Std. Error	Lower	Upper
b0	1967.656	0.017	1967.624	1967.688
b1	0.395	0.005	0.384	0.405
b2	0.425	0.009	0.408	0.442
b3	-0.043	0.024	-0.090	0.003
b4	224.113	0.034	224.046	224.180
b5	1.032	0.047	0.941	1.123
b6	-0.092	0.031	-0.152	-0.032
b8	0.280	0.073	0.136	0.423
b9	0.752	0.115	0.526	0.979
b10	0.845	0.000	0.845	0.845
b11	0.790	0.113	0.569	1.011
b12	0.688	58.014	-113.147	114.523
b13	0.951	0.101	0.753	1.149
b14	1.426	0.014	1.399	1.453
b15	1.124	0.024	1.077	1.172
b16	0.691	0.027	0.639	0.743

Figure 2 LOCATION variable – Quartic Polynomial Surface

Figure 3 N_B_HOOD Variable – Kriged residuals

